

BACKGROUND READING FOR BEGINNERS

Here we list general references suitable for non-specialists who wish to learn more about algebraic combinatorics in general, or Kostka polynomials in particular.

1. GENERAL BACKGROUND BOOKS IN ALGEBRAIC COMBINATORICS

- (1) Lynne Butler, *Subgroup lattices and symmetric functions*. Mem. Amer. Math. Soc. 112 (1994), no. 539, vi+160 pp.
NO ANNOTATION AVAILABLE YET.

- (2) William Fulton, *Young Tableaux*. Cambridge University Press, 1996.

This book contains a thorough discussion of the algebra and combinatorics of Young tableaux. Part 1 of the book discusses fundamental combinatorial tableaux constructions including bumping (RSK insertion), sliding (jeu-de-taquin), RSK correspondences, Schur functions, and the Littlewood-Richardson rule. Part 2 shows how tableaux arise in the representation theory of symmetric groups and general linear groups. Part 3 discusses the role of tableaux in the geometry of Grassmannians and flag manifolds. As one proceeds from Part 1 to Part 2 to Part 3, the difficulty level of the book increases quite substantially. Part 1 is self-contained (no prerequisites), but the same cannot be said for parts 2 and 3.

- (3) Ian Macdonald, *Symmetric Functions and Hall Polynomials* (second edition). Oxford University Press, 1995.

This book is the standard encyclopedic reference for symmetric functions, Hall-Littlewood polynomials, and Macdonald polynomials. Macdonald's viewpoint is highly algebraic, definitely NOT combinatorial, which may make the book tough reading for more combinatorial-minded readers. A huge amount of information from the literature is presented in the form of long exercises at the end of each section (called “examples” by Macdonald). I would hesitate to recommend this book as initial reading for beginners (e.g. graduate students). Read Sagan, Fulton, and Stanley first instead.

- (4) Bruce Sagan, *The Symmetric Group: Representations, Combinatorial Algorithms, and Symmetric Functions* (second edition). Springer, 2001.

This book is a highly readable introduction to the representation theory of symmetric groups, combinatorial algorithms on tableaux such as the RSK algorithm, and symmetric functions. Technical prerequisites are minimal — one only needs to know standard group theory and linear algebra.

- (5) Richard Stanley, *Enumerative Combinatorics* (2 volumes). Cambridge University Press.

This is the standard encyclopedic reference for enumerative combinatorics. Chapter 7 of Volume 2 (and the appendix) also contains a good deal of algebraic combinatorics and information about symmetric functions.

2. SURVEY ARTICLES RELEVANT TO THE KOSTKA WORKSHOP

- (1) Adriano Garsia and Jeff Remmel, “Breakthroughs in the theory of Macdonald polynomials,” *Proc. Natl. Acad. Sci. USA* **102** # 11 (2005), 3891—3894.

This is a nice survey article that gives a lot of historical background on Schur functions, Hall-Littlewood polynomials, and Macdonald polynomials.

(2)